

A comprehensive review of spike sorting algorithms in neuroscience

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Highlights

- The detailed steps of spike sorting algorithm and the different algorithms used in each step are summarized.
- The advantages and disadvantages of each step of spike sorting algorithm are compared.
- The detailed application of deep learning technology in spike sorting is introduced.

Abstract

Spike sorting plays a pivotal role in neuroscience, serving as a crucial step of separating electrical signals recorded from multiple neurons to further analyze neuronal interactions. This process involves separating electrical signals that originate from multiple neurons, recorded through devices like electrode arrays. This is a very important link in the field of brain-computer interfaces. The objective of spike sorting algorithm (SSA) is to distinguish the behavior of one or more neurons from background noise using the waveforms captured by brain-embedded electrodes. This article starts from the steps of the conventional SSA and divides the SSA into three steps: spike detection, spike feature extraction, and spike clustering. It outlines prevalent algorithms for each phase before delving into two emerging technologies: template matching and deep learning-based methods. The discussion on deep learning is further subdivided into three approaches: end-to-end solution, deep learning for spike sorting steps, and spiking neural networks-based solutions. Finally, it elaborates future challenges and development trends of SSAs.

Keywords: Spike sorting, spike detection, feature extraction, clustering, deep learning

Introduction

The control signals currently used in brain-computer interfaces (BCI) mainly include the following five types: action potentials (spike), local field potentials, electrocorticography (ECoG), epidural field potentials, and electroencephalography [1]. The sites where each signal is acquired in the brain are shown in **Figure 1**. **Figure 1** was adapted from [1]. Spike is a key signal reflecting the behavioral activity of the brain, and the study of neuronal information storage and encoding via spike contributes to better development of analog brain comput-

ers [2]. There is a close relationship between local field potentials and spike, and their good stability and frequency content provide key advantages for long-term, low-power BCI [3]. ECoG, capturing detailed aspects of actual and imagined body movements, facilitates the development of robust and long-term BCI systems [4]. Compared to ECoG, epidural field potentials are acquired in the epidural space, which greatly reduces the risk of surgical complications, making them suitable for long-term implantation of BCI [5]. though non-invasive and low-cost, offers limited brain activity information, restricting its use to simple communication and

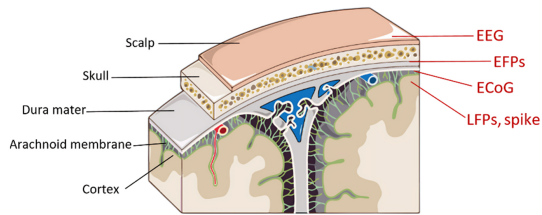


Figure 1. The locations in the brain where various signals occur. EEG, electroencephlography; EFPs, eqidural field potentials; ECoG, electrocorticogra-phy; LFPs, local field potentials. This Figure was adapted from [1].

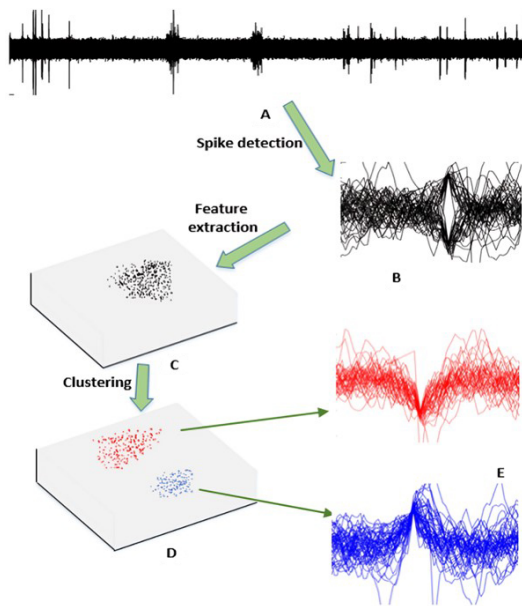


Figure 2. Basic steps for spike sorting. (A) A piece of filtered neuronal signal; (B) Spikes are detected, usually using an amplitude threshold of signal; (C) Spike features are extracted to achieve a dimensionality reduction; (D) Clustering operation based on extracted features; (E) The clustering algorithm classifies the waveforms and associates each cluster with a unit. This figure was adapted from [17].

control tasks [6]. Other signals have also been used in BCI, including near-infrared spectroscopy of brain blood flow and functional magnetic resonance imaging. The former's poor spatial resolution and the latter's poor temporal resolution, coupled with high costs, rendering them impractical for widespread application in BCI technologies.

In general, there is a correlation between the level of invasiveness of neural recordings and the quality of signal obtained as well as spatial, spectral, and temporal resolution. The higher the level of invasiveness, the more brain information can be obtained [7]. Spikes, directly emitted by the cells at the implantation site with a frequency range generally between 300Hz and 6000Hz, can reflect the interaction

between high-level brain functions and single neurons [8]. Typically, spikes are captured by inserting high-impedance electrodes with a diameter of several microns into the brain, thereby recording neuronal activity near the electrodes in the range of 50-100 microns [9]. In recent years, BCI using spike has attracted increasing interest from scientific community, with the goal of mapping, assisting, enhancing, and repairing cognitive or sensorimotor functions in human or animal brains. Today, spikes are used in the field of BCI to detect pain signals, control robotic arms or wheelchairs, and treat spinal cord injuries [10-12]. However, due to the large amount of spike data and low signal-to-noise ratio (SNR), it has not been widely used clinically.

Since the 1970s, the accurate extraction, detection, and the classification of spikes has been a hot topic in the neuroscience field, known as spike sorting [13]. This review provides a general overview of spike sorting, introduces corresponding algorithms for different steps, and summarizes and compares the current mainstream algorithms. Finally, current study limitations are summarized, and future developments are projected.

Conventional spike sorting algorithm (SSA)

Spike sorting is an algorithm to detect individual spikes from extracellular neural recordings and classify them based on their shape. The algorithm classifies the detected spikes as originating neurons [14]. The SSA works by dividing different neurons into different clusters, according to their different electrical proximity to the recording electrode and different shapes of dendrites [15]. In theory, a single neuron is represented by a single cluster; however, due to interactions among different neurons, the obtained spike information often overlaps, resulting in a large number of false positives in classification across adjacent channels, thereby complicating accurate categorization [16]. As shown in **Figure 2**, traditional spike sorting has three main steps. **Figure 2** was adapted from [17]. The first step, spike detection, involves identifying spikes at the corresponding time points based on the waveform of each spike. The second step is to extract features corresponding to different spikes and convert them into another feature domain. The final step, spike clustering, is to classify the spikes into different clusters [13].

Spike detection

Spike detection is the initial phase of SSA, ded-

icated to isolating individual spikes from continuous neural recordings, setting the groundwork for the subsequent stages of the sorting process. Generally, the duration of a spike event is usually 1-3 ms, and the sampling time of each spike event lasts for 30-90 sampling points to prevent spikes from being repeatedly detected. There are currently three mainstream methods of spike detection, including threshold detection method, nonlinear energy operator method, and wavelet transform product method. Each of these methods has its own advantages and disadvantages [17, 18].

Amplitude thresholding

The most straightforward algorithm is to apply an amplitude threshold to the spike signal. Since the filtered signal is easily visualized on top of background noise activity, this method is resource-intensive and computationally fast. However, if the applied threshold is too small, noise fluctuations will cause false positive events, and some spikes will be missed. Therefore, setting an adaptive threshold is more suitable.

The most reasonable way is finding a multiple k of the noise σ_n as the threshold, that is $Thr=k\sigma_n$. The general value of k is between 3 and 5. σ_n can also be other values. A threshold estimation formula based on the signal median is given [19],

$$Thr = 4 \times \text{median}\left(\frac{|x|}{0.6745}\right) \quad (1)$$

where 0.6745 comes from the inverse function of the standard normal distribution cumulative function, which has a value of 0.75. This method processes the background noise according to the standard Gaussian distribution. Even though the noise distribution in real world may deviate from the Gaussian distribution, it has been confirmed that this median-based estimation is more accurate than the standard deviation estimation [20]. However, Equation (1) is not suitable for all situations.

Another study proposed an improved formula [21],

$$Thr = \frac{\text{median}\left\{\frac{|x|}{0.6745}\right\} \sqrt{2 \log_2(n)}}{1.6} \quad (2)$$

where n is the length of the detected data. The addition of n into Equation (2) reduces the mixed noise interference introduced by the col-

lection environment, making it more suitable for the adaptive threshold algorithm [21]. However, Equation (2) was later proved to be unsuitable for detection of high noise levels [22]. In this context, Equation (3) was proposed, as follows:

$$Thr = \text{median}\left(\frac{|x|}{0.6745}\right) \sqrt{\frac{\log_2(n)}{n} \left(\frac{\ln n}{\ln 2}\right)^3 q} \quad (3)$$

Equation (3) reduces the interference caused by noise fluctuations, making the set threshold more robust. It has been experimentally confirmed that under higher noise levels, the detection accuracy of Equation (3) is significantly higher than Equation (1) and (2) [22].

Nonlinear energy operator (NEO)

The NEO is a more powerful detection method, leveraging both frequency and amplitude information. This capability renders NEO more effective than the threshold method in low SNR situations [23]. For the continuous sampling signal $x(n)$, its discrete time NEO ϕ is shown in Equation (4). In addition, some studies suggest using smoothing windows to convolve NEO time series, which can reduce the probability of false positives.

$$\phi[x(n)] = x^2(n) - x(n+1) \times x(n-1) \quad (4)$$

$$Thr_{NEO} = \frac{8}{N} \sum_{n=1}^N \phi[x(n)] \quad (5)$$

Spike is the component with the highest energy in the entire collected signal. Compared with the noise signal, the energy of the spike signal increases instantaneously. This method is ideal for on-chip implementation due to its good transient and computational properties [23]. Malik et al. provided a method for NEO threshold judgment, as shown in Equation (5), whereby a value surpassing this threshold is classified as a spike [24].

Wavelet transform product

Wavelet transform has also been proposed for spike detection due to its ability to integrate information from both the time and frequency domains [25]. Compared with the first two methods, the wavelet transform method does not regard the background noise as a standard Gaussian distribution [26]. The principle of this method mainly exploits the fact that the wavelet function is a long "peak" waveform. When sliding wavelet decomposition is used, its essence

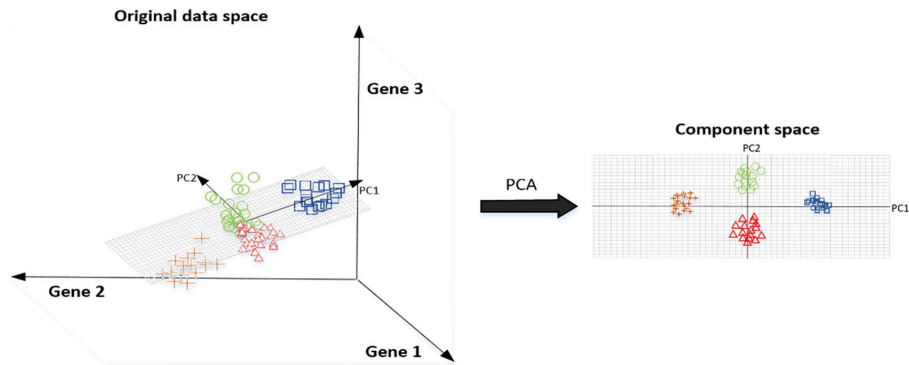


Figure 3. The process of PCA dimensionality reduction. PCA, principal component analysis. This Figure was adapted from [42].

is a “template matching” process to evaluate the similarity between the wavelet function and spike. The mathematical definition of wavelet transform is shown in Equation (6), where ψ is the wavelet function, τ is the translation scale, and α is the scale factor.

$$W(\alpha, \tau) = \int_{-\infty}^{\infty} x(t) \frac{1}{\alpha} \psi\left(\frac{t-\tau}{\alpha}\right) dt \quad (6)$$

$$P(n) = \prod_{j=j_{max}-2}^{j_{max}} |w(2^j, n)| \quad (7)$$

It identifies the signal segment as a spike when there is a relatively high similarity between the signal segment and the wavelet function. There are many choices for wavelet functions in spike detection, such as Haar wavelet, db4 wavelet, and Biorthogonal wavelet. In applications, discrete wavelet transform is generally used, where the value of α is $2^j(j=1,2,3\dots)$. First, the wavelet coefficient $w(\alpha, \tau)$ corresponding to each j value for each time point is calculated, and all time points until the set maximum j value are summed up, termed as j_{max} . Next, the value of $P(n)$ is calculated, which is essentially the product of the wavelet coefficients across three consecutive scales, as shown in Equation (7). Similar to the method described above, using a smoothing window to convolve the $P(n)$ sequence can reduce spurious spike due to cross terms and background noise [27, 28].

Among the above three spike detection technologies, since the first two have relatively low computing resource requirements for hardware implementation, they are often favored for on-line implementation. When the SNR is high and computing resources are limited, the threshold detection method is more suitable. Although the NEO has a simple structure, it necessitates

data storage and introduces delays. The first two methods are prone to false positives and false negatives as the noise level changes. Without considering the amount of computing resources, the wavelet transform method can yield the best results [29, 30].

Spike feature extraction

Feature extraction can be performed from three aspects: time domain features, transformation domain features, and dimensionality reduction features. For the time domain features, actual operation can be performed based on the geometric features and derivative features of the spike [31, 32]. For transformation domain features, techniques such as Fourier transform, Hilbert transform, and wavelet transform are employed [33-35]. For dimensionality reduction features, principal component analysis (PCA), linear discriminant analysis (LDA), and Laplacian eigenmaps are utilized [36-38]. After feature extraction, 2 to 3 key features are generally selected and used as inputs in the clustering algorithm to ensure that the next step of the clustering algorithm can be effectively implemented [39, 40]. Several mainstream spike feature extraction algorithms are introduced below.

PCA

PCA is the most commonly used method in current feature extraction. Its essence is a dimensionality reduction method that projects a data set with multiple relevant features into a coordinate system with fewer relevant features. All detected spike time samples are used as input $x(n)$, and the covariance matrix is eigenvalue decomposed, where the eigenvectors represent the projection direction of the original data. The algorithm mainly includes three steps: (1) creating the covariance matrix of the data set;

(2) calculating all eigenvalues of the covariance matrix and retaining the first k eigenvalues in descending order of variance; (3) transforming the data points through k feature vectors [41].

Figure 3 shows the dimensionality reduction on the original data through PCA. **Figure 3** was adapted from [42]. The disadvantage of this method is its tendency to lose information as the complexity of the collected spike data increases. It is stated that when a higher k value is selected, the variance of the higher component may be affected by the background noise, so this method is not suitable for feature extraction where the spike information is rich [13].

Features of wavelet transform

Wavelet transform is an integral transform that decomposes a specific signal into the sum of different wavelet signals. The relevant equations of wavelet transform are presented in Section 2.1.3. Through the low-frequency and high-frequency wavelet coefficients, it can accurately depict the spike shape [43]. Generally, wavelet transform convolves the original signal with wavelet functions of different parameters derived from the mother wavelet, which can quantify the details of the signal at different resolutions [35]. Haar wavelet and Daubechies wavelet are the two most commonly used mother wavelets in analyzing neurophysiological signals due to their orthogonality. They are able to identify the characteristics of a spike through a few wavelet coefficients without making a priori assumptions about the shape of the spike [19, 44, 45].

The features that can be extracted from the time spectrum mainly include extreme value features and energy distribution features. The former is the most prevalent feature, involve extracting the peak amplitude across each scale and correlating them with the corresponding scale parameters and translation parameters to construct a comprehensive feature vector. The latter requires calculating the energy distribution of each scale space from the energy spectrum, and then identifying the corresponding scale parameters and translation parameters to form the feature vector [46].

LDA

LDA is a linear projection technology that seeks a suitable projection direction within a low-dimensional space, so as to maximize the distance between different categories and minimize the distance between the same categories [47]. LDA first calculates the covariance matrix

of the data and performs eigenvalue decomposition of the covariance matrix. Then, a projection matrix is formed based on the obtained eigenvectors and eigenvalues to map the original data into a new low-dimensional space [48]. LDA needs to clearly minimize the inter-class variance and maximize the inter-class variance, which are shown in Equation (8) and Equation (9), respectively. Here, x_i is the i th data point in the k th cluster c_k , μ_k represents the average of data points in the k th cluster, μ represents the average of all data points, and n is the total number of data.

$$S_W = \sum_{k=1}^K \sum_{x_i \in c_k}^{n_k} (x_i - \mu_k)(x_i - \mu_k)^T \quad (8)$$

$$S_b = \frac{\sum_{k=1}^K n_k (\mu_k - \mu)(\mu_k - \mu)^T}{n} \quad (9)$$

LDA has demonstrated its effectiveness in separating spike features, especially when the SNR is low [48].

Unlike PCA, which simplifies high-dimensional data into two or three dimensions without significant information loss and facilitates visualization and classification identification, LDA optimizes dimensionality reduction to avoid overfitting. Wavelet transform can extract detailed features in the spike without too much information loss. However, PCA does not account for the categorical relationships between data points and relies solely on variance for determining principal components, leading to potential information loss. The classification effectiveness of LDA can easily be compromised when there is a great overlap between the data distribution of different categories. Wavelet transform is easily affected by noise, thus selecting suitable parameters for the wavelet basis function is essential [49-51].

Spike clustering

Spike clustering refers to organizing points in the feature space into clusters. Each cluster is associated with a different neuron, separated by defined boundaries between different clusters [52]. Optimal clustering techniques should minimize user intervention and achieve efficient and accurate results. It is generally believed that the changes within the cluster are caused by the noise superimposed on the real spike waveform [53]. The background noise obeys the Gaussian distribution. Therefore, most clustering algorithms are built based

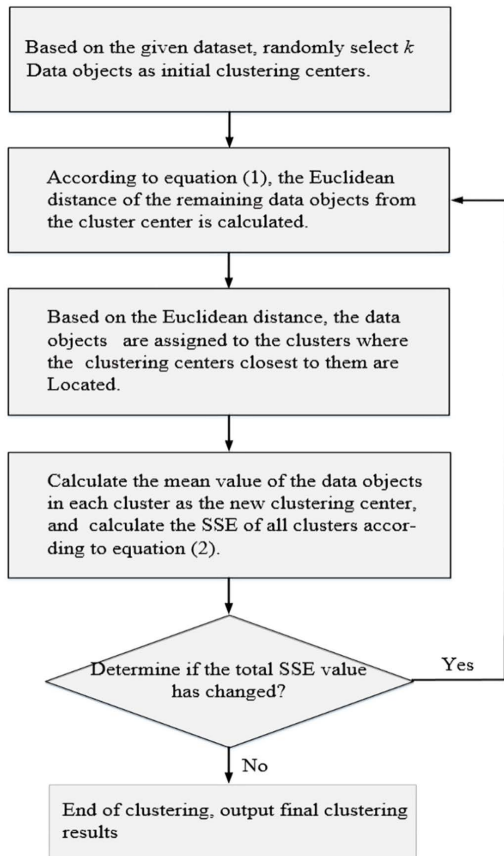


Figure 4. K-means algorithm flow chart. SSE, sum of squared error. This figure was adapted from [53].

on the Gaussian model. Most SSAs perform clustering by fitting a Gaussian mixture model, modeling the feature density curve as a sum of Gaussians, or fitting a mixture of t distributions. Several clustering methods commonly used in recent years are introduced.

K-means

K-means clustering is one of the prevalent unsupervised learning techniques. It primarily uses the Euclidean distance $d(x, c_i)$ as an indicator to measure the similarity between data objects. Its calculation formula is shown in Equation (10), where x is the data object, c_i is the i th cluster center, and m is the dimension of the data. The similarity is inversely proportional to the distance between data objects.

$$d(x, C_i) = \sqrt{\sum_{j=1}^m (x_j - C_{ij})^2} \tag{10}$$

$$SSE = \sum_{i=1}^k \sum_{x \in C_i} |d(x, C_i)|^2 \tag{11}$$

The algorithm needs to specify the initial number of clusters k and k initial cluster centers in advance. Then, based on the similarity between the data object and the cluster center, the location of the cluster center is continuously updated, and the sum of squared error of the cluster is reduced, as shown in Equation (11). When the sum of squared error no longer changes or the objective function converges, clustering ends and the final result is obtained [54, 55]. The K-means algorithm is a continuously iterative process, and its algorithm flow is shown in Figure 4. Figure 4 was adapted from [53].

Mean shift

Mean shift is a non-parametric clustering method first proposed by Fukunaga and Hostetler [56]. It treats data samples as empirical representations of probability density functions in a d -dimensional feature space. Dense regions in the d -dimensional feature space is used to represent local maxima of the underlying distribution [57]. The algorithm first estimates the kernel density function, as shown in Equation (12), where k represents the symmetrical kernel function, which usually is a Gaussian function.

$$f(x) = \sum_i k\left(\frac{\|x - x_i\|}{h}\right) \tag{12}$$

After each data point is assigned to the corresponding $f(x)$, the algorithm moves the data point to the KDF mapping according to the gradient function in Equation (13) [58].

$$\nabla f(x) = \frac{2c_{k,d}}{nh^{d+2}} \left[\sum_{i=1}^n k'\left(\frac{\|x - x_i\|}{h}\right) \left[\frac{\sum_{i=1}^n x_i k'\left(\frac{\|x - x_i\|}{h}\right)}{\sum_{i=1}^n k'\left(\frac{\|x - x_i\|}{h}\right)} - x \right] \right] \tag{13}$$

The focus of the mean shift algorithm is primarily to improve calculation efficiency and robustness [15]. In recent research, Yang et al. proposed a method that combines the mean shift algorithm with the optical flow method, which reduces the cumulative error and thereby improves computational efficiency [59].

Super-paramagnetic clustering (SPC)

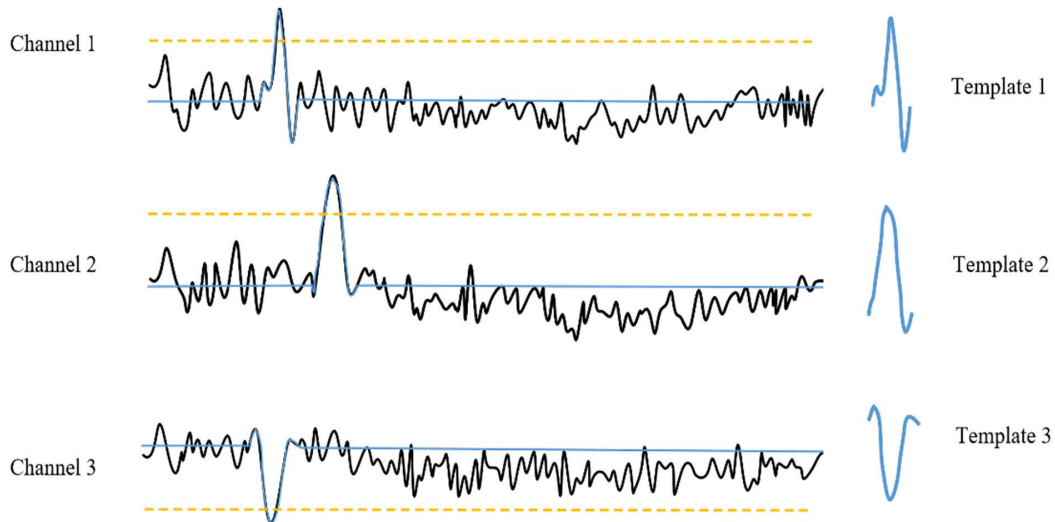


Figure 5. Templates are obtained using threshold detection method. This figure was adapted from [15].

SPC is an unsupervised classification technique based on clustering self-tenancy of data density and interaction energy. Drawing inspiration from the interactions observed among superparamagnetic particles under varying temperatures, SPC distinguishes itself from conventional algorithms by excluding the use of clustering distribution functions. First, it uses Equation (14) to mathematically simulate the interaction between x_i and x_j at different points, where a is the average distance between nearest neighbor points. Then, it assigns a “Potts spin” state variable s from 1 to q to each point x_i , where q is usually chosen to be 20. Finally, it uses the Wolff algorithm to perform N Monte Carlo iterations at different temperatures [19, 60]. The state value p_{ij} is updated according to Equation (15), where T represents the temperature value.

$$J_{ij} = \frac{1}{k} \exp\left[-\frac{|x_i - x_j|^2}{2a^2}\right] \quad (14)$$

$$P_{ij} = 1 - \exp\left(-\frac{J_{ij}}{T} \delta_{s_i, s_j}\right), \delta_{s_i, s_j} = \begin{cases} 1 & \text{if } s_i = s_j \\ 0 & \text{otherwise} \end{cases} \quad (15)$$

$$G_{ij} = \frac{(q-1)c_{ij} + 1}{q} \quad (16)$$

s will be iteratively updated according to the value of p_{ij} until it becomes stable. Equation (16) introduces the spin-spin correlation function, where c_{ij} is a number belonging to the interval

[0, 1]. An appropriate threshold ε can be selected. When $G_{ij} > \varepsilon$, different data points x_i and x_j belong to the same cluster.

Fuzzy C-means (FCM)

FCM combines the K-means algorithm with fuzzy logic, which has good processing effects on data with high complexity. FCM is an iterative algorithm whose execution steps are similar to K-means. First, the number of clusters k needs to be determined. Its value can be fixed or adaptive. Next, it randomly initializes the value μ_{ij} of the cluster member of each point x_i relative to the cluster center C_j , and then calculates the cluster center according to Equation (17) [15, 61].

$$C_j = \frac{\sum_{i=1}^D \mu_{ij}^m x_i}{\sum_{i=1}^D \mu_{ij}^m} \quad (17)$$

$$\mu_{ij} = \frac{1}{\sum_{k=1}^N \left(\frac{\|x_i - c_j\|}{\|x_i - c_k\|}\right)^{\frac{2}{m-1}}} \quad (18)$$

where D is the number of data points, and N is the number of clusters, and m is the fuzzy parameter. The values of cluster members are then calculated and updated using Equation (18), where m is a parameter greater than 1. When m approaches 1, the ambiguity decreases, and the algorithm result approaches the

K-means algorithm.

Of the four algorithms introduced above, K-means has the simplest structure and is easy to implement, excelling in efficiency with large datasets. Mean shift has good adaptability to data with linear structure. SPC stands out for good adaptability to automatically determine the number of clusters. FCM is distinguished by its good robustness in data processing and has good adaptability to situations where data points belong to multiple clusters. However, each algorithm has its limitations: K-means is sensitive to noise and outliers, and thus does not have good robustness; Mean shift has high computational complexity on large-scale data sets; SPC is complex and can be affected by temperature, and the convergence speed of FCM is relatively slow [62-65].

Novel SSAs

Novel SSAs do not follow the three steps of traditional algorithms. For example, using neural system simulation and deep shrinkage automatic encoding methods to perform spike sorting [66, 67]. Current mainstream algorithms can perform two or more steps simultaneously, thereby improving algorithm efficiency. These algorithms are mainly divided into two categories, one is template matching and the other is deep learning.

Template matching

Template matching identifies the position of a specific template within a signal sequence, facilitating accurate and efficient locate specific spikes in spike sorting. It takes the normalized-template-matching method proposed as an example [68]. Firstly, conventional SSAs are used to extract the initial template, such as threshold detection, as shown in **Figure 5**. The figure was adapted from [15]. Subsequently, the template was used to move against the neural recording to assess waveform similarity that determined by calculating the relationship between the extracellular voltage signal and the average spike waveform of each candidate single unit, which here called cross-correlation. Let the average spike waveform of all channels be μ_i , where $\mu_i = [\mu_{i,1}, \mu_{i,2}, \dots, \mu_{i,N}]$, $\mu_{i,n}$ is at the average spike wave in n channels. Let the $L = f_s k$, where f_s is the sampling frequency and k is the length of the custom time window, then $\mu_{i,n}$ is a $1 \times L$ vector. In the same way, the neural recording signal is defined as a vector $u_{i,n}$ that changes with time, thus obtaining $V(t) = [u(t)_1, u(t)_2, \dots, u(t)_N]$. Based on the above, the cross-correlation equation can be obtained:

$$C_i(t) = V(t) \times \mu_i^T \quad (19)$$

Based on cross-correlation, the two steps of spike detection and feature extraction can be accomplished, and then K-means and other methods can be employed to complete clustering and the entire SSA step. However, since neural recording signals are usually non-stationary, template matching methods require template recalibration over a period of time.

Recent advancements in template matching for peak sorting include the utilization of particle swarm optimization algorithm and the multi-template matching method to optimize the template [69, 70]. For the optimized template, experimental results demonstrated that it could significantly reduce the occurrence of false positives and false negatives. Another study combined templates with convolutional neural networks (CNNs), employing CNNs to train on real spikes and overlapping spikes, which allows for correct spike classification and minimizes the occurrence of repeated spikes [71].

Deep learning

Deep learning is a popular technology that has been used in various fields for several years. It involves the application of machine learning through deep artificial neural networks (ANN), which has more layers, parameters and neurons. The use of deep learning methods to solve the peak sorting problem has become a popular research direction, and there are three main strategies: (1) end-to-end solution, (2) deep learning for spike sorting steps, and (3) spiking neural network (SNN)-based solutions [72-74].

End-to-end solution

The end-to-end solution uses the filtered neural recording as the input of the deep neural network and directly outputs the spike sequences produced by different neurons. This approach eliminates tedious preprocessing steps by starting from raw data as input. For instance, researchers used CNN and long short-term memory to perform peak sorting in an end-to-end manner [75]. Here, CNN is used for spike detection, and long short-term memory is used to receive the output stream of CNN and process the corresponding information. Other researchers proposed a medium 1D-CNN model tailored for single-channel spike sorting [76]. Although the end-to-end solution is a simple and

efficient way, its internal parameters require a large amount of data for training, and this method is not suitable for complex spikes.

Deep learning for spike sorting steps

Section 2 explains spike sorting as a process comprised three independent steps. Some of these steps can be improved by using deep learning methods. The most common one is to use deep learning for spike detection and denoising. Extracellular nerve signal recording contains a variety of components originating from the signal recording equipment or the measured organism itself, such as the activity of nearby neuronal cells. These noises can affect the detection accuracy. Lecoq et al. used original noise samples to train a spatiotemporal nonlinear difference model, thereby achieving the effect of eliminating independent noise sources in the input signal [77]. Okreghe et al. proposed a deep spike detection technique using CNN in conjunction with K-means, exhibiting robust learning capabilities for high-dimensional vectors and effective removal of artifacts in the acquisition channel [78].

SNN-based solutions

SNN, a relatively new type of neural network, exhibits functions more akin to neural networks in living organisms when compared to other conventional neural networks. SNN uses a temporal encoding scheme to encode information into spike sequences. It has more powerful information representation capabilities than ANN, especially for complex temporal or spatiotemporal data. In hardware implementation, SNN can achieve fast and large-scale parallel information processing [79, 80]. In the application of spike sorting, Mukhopadhyay et al. proposed a spike sorting method that combines SNN and K-means to achieve training and classification of on-chip systems through a two-step shared training scheme [81]. Werner et al. proposed a method to implement spike sorting using a two-layer SNN. In this technology, there is no need for preliminary waveform detection. The first layer is used to filter the original signal, and the second layer is used for detection and feature extraction. Both layers of neurons follow the Leaky Integrate-and-Fire model [82]. The disadvantage of this technology is that the parameters of Leaky Integrate-and-Fire need to be manually adjusted to adapt to different shapes of waveforms. Later, Bernert et al. optimized it and confirmed the high efficiency of this technology in high-density electrode settings [83].

Conclusion

This review provides a detailed introduction of various steps involved in SSA, covering the predominant algorithms associated with each step and their current research status. Additionally, a detailed description of the application of deep learning technology in the field of spike sorting is provided. With the development of BCI, there is an escalating demand for enhanced neural signal acquisition channels and signal quality, which also poses challenges to the development of SSAs.

The foremost challenge is to solve the problem of signal non-stationarity. Neural signals change over time and can be affected by multiple factors, leading to temporal variations in spike shapes, especially in systems that require manual intervention [84, 85]. The second challenge is overlapping spikes, which significantly reduce the performance of conventional clustering algorithms [86]. The most commonly accepted solutions nowadays are Bayesian statistical techniques and template matching introduced in section 3.1 and the ANN. However, the above methods are computationally intricate and demand substantial hardware capabilities. Therefore, future research should aim to simplify and enhance the efficiency of algorithms designed to tackle overlapping spikes. The third challenge is the determination of the training data set and evaluation scheme. Most current spike sorting systems are evaluated using synthetic datasets with real labels. The simplest method is to add modeled Gaussian noise to the spike waveform. Due to the interactions between neuronal cells, it is very challenging to form realistic multi-channel synthetic data.

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